Enhancing Semi-Supervised Clustering: A Feature Projection Perspective

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ABSTRACT

Semi-supervised clustering employs limited supervision in the form of labeled instances or pairwise instance constraints to aid unsupervised clustering and often significantly improves the clustering performance. Despite the vast amount of expert knowledge spent on this problem, most existing work is not designed for handling high-dimensional sparse data. This paper thus fills this crucial void by developing a Semi-supervised Clustering method based on spheRical KmEans via fEature projectioN (SCREEN). Specifically, we formulate the problem of constraint-guided feature projection, which can be nicely integrated with semi-supervised clustering algorithms and has the ability to effectively reduce data dimension. Indeed, our experimental results on several real-world data sets show that the SCREEN method can effectively deal with high-dimensional data and provides an appealing clustering performance.

Categories and Subject Descriptors

H.2.8 [Database Management]: Database Applications -Data Mining; I.5.3 [Pattern Recognition]: Clustering

General Terms

Algorithms, Experimentation

Keywords

Semi-Supervised Clustering, Pairwise Instance Constraints, Feature Projection

1. INTRODUCTION

Semi-supervised clustering, learning from a combination of labeled and unlabeled data, has recently become a topic of significant interest to data mining and machine learning communities. Indeed, in many application domains, additional information such as some labeled instances or pairwise instance constraints are available and can be used to aid the unsupervised clustering process [4, 5, 10, 25, 26].

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Existing methods for semi-supervised clustering can be generally grouped into three categories. First, the *constraintbased* methods aim to guide the clustering process with pairwise instance constraints [25] or initialize cluster centroids by labeled instances [4]. Second, the *distance-based* methods employ metric learning techniques to get an adaptive distance measure used in the clustering process based on the given pairwise instance constraints [26]. Finally, the *hybrid* method proposed by Basu et al. [5] unifies the first two methods under a general probabilistic framework.

However, most existing semi-supervised methods are not designed for handling high-dimensional data. It is wellknown that the traditional Euclidean notion of density is not meaningful in high-dimensional data sets [7]. Since most semi-supervised clustering techniques are based on proximity or density, they often have difficulties in dealing with high-dimensional data. Therefore, it is necessary to integrate feature reduction into the process of semi-supervised clustering. The key challenge is how we can incorporate supervision into dimensionality reduction such that the reduced data can still capture the available class information.

To this end, we propose a Semi-supervised Clustering method based on spheRical K-mEans via fEature projectioN (SCREEN). Specifically, we first formulate the problem of constraint-guided feature projection and provide an analytical solution to the associated optimization problem. Then, we exploit this constraint-guided feature projection technique to reduce the dimensionality of the original dataset and use constrained spherical K-means algorithm on the low-dimensional projected data for clustering.

In this paper, we consider supervision provided in the form of must-link and cannot-link constraints on pairs of instances. A *must-link* constraint means that the pair of instances involved must reside in the same cluster while a *cannot-link* constraint means that the pair of instances should always be placed in different groups. Indeed, the use of must-link and cannot-link constraints is a natural and practical choice, because the labeled instances may not be available and are harder to collect than pairwise constraints. For example, in the context of clustering GPS data for lanefinding [25] or grouping different actors in movie segmentation [3], the complete class information may not be available in these cases, but the pairwise instance constraints can be extracted automatically with minimal effort. Also, a user who is not a domain expert is more willing to provide an answer to whether two objects are similar/dissimilar more than to specify explicit labels. Moreover, pairwise instance constraints are more general than class labels in that we

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can always generate equivalent pairwise instance constraints from labeled instances, but not vice versa.

Finally, we have conducted experiments on some realworld datasets from different application domains. Our experimental results show that, for high-dimensional data, the SCREEN method can achieve better clustering performance than the state-of-the-art, semi-supervised clustering methods. In addition to this, we provide an analysis on the relative importance of *must-link* and *cannot-link* constraints. This analysis indicates that *cannot-link* constraints are much more important than *must-link* constraints in providing supervision for the clustering process.

Overview. The remainder of this paper is organized as follows. In Section 2, we introduce the general framework of our proposed SCREEN algorithm. Section 3 discusses the experimental results on several real-world datasets. Related work on the existing methods of semi-supervised clustering is discussed in Section 4. Finally, in Section 5, we draw conclusions and make suggestions for future work.

Table 1: Summary of notations.

Symbols	Description	
N	number of instances in the original dataset	
K	number of pre-specified clusters	
$\mathcal{X} = \{x_i\}_1^N$	set of N unlabeled instances	
$U = \{\mu_i\}_1^K$	set of K cluster centroids	
C_{ML}	set of <i>must-link</i> constraints	
C_{CL}	set of <i>cannot-link</i> constraints	
$C_{d \times m}$	difference matrix formed by C_{CL}	
$M_{m \times m}$	covariance matrix of $C_{d \times m}$	
$F = \{F_l\}_1^k$	projection matrix calculated from $M_{m \times m}$	
ξ_l	corresponding eigen value of F_l	
β	ratio between <i>must-links</i> and <i>cannot-links</i>	

2. THE SCREEN METHOD

Before we describe the SCREEN method, we summarize the main notations used in this paper in Table 1.

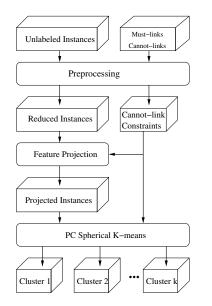


Figure 1: The Framework of the SCREEN Method.

Figure 1 shows the framework of the SCREEN method. Given a set of instances and a set of supervision in the form of must-link constraints $C_{ML} = \{(x_i, x_j)\}$ where (x_i, x_j) must reside in the same cluster, and cannot-link constraints $C_{CL} = \{(x_i, x_j)\}$ where (x_i, x_j) should be in the different clusters, the SCREEN method is composed of three steps. In the first step, a pre-processing method is exploited to reduce the unlabelled instances and pairwise constraints according to the transitivity property of must-link constraints. In the second step, a constraint-guided feature projection method, called SCREEN_{PROJ}, is used to project the original data into a low-dimensional space. Finally, we apply a version of semi-supervised clustering algorithms based on constrained spherical K-means on the projected low-dimensional dataset to produce the clustering results.

The rest of this section is organized as follows. In Section 2.1, we introduce our initialization method for the unlabeled instances and pairwise constraints in detail. Section 2.2 presents the constraint-guided feature projection method– SCREEN_{PROJ}–which gives an analytical solution to the optimization problem in finding the projection matrix. Finally, in Section 2.3, we describe our semi-supervised clustering based on constrained spherical K-means to produce the final clustering results.

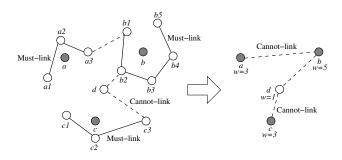


Figure 2: An Illustration of Initialization.

2.1 Initialization

If there is no error in the pairwise constraints, it is easy to demonstrate that the *must-link* constraints represent an equivalence relation. This enables us to replace each transitive closure of *must-link* constraints with its average instance as demonstrated in Figure 2, where the solid line represents the *must-link* constraint and the dashed line represents the cannot-link constraint. In Figure 2, original instances are shown in white nodes and the average instances of transitive closures are represented by grey nodes. Sets $\{a_1, a_2, a_3\}$, $\{b_1, b_2, b_3, b_4, b_5\}$, and $\{c_1, c_2, c_2\}$ represent different transitive closures forced by *must-link* constraints. After initialization, we can eliminate all *must-link* constraints and use the average instances a, b and c in each closure to represent the original *cannot-link* constraints. In the transformed dataset, the size of each transitive closure becomes the weight of the representative instance. Note that if there are some erroneous constraints, we need to identify and remove them in the initialization step. However dealing with the mis-specified constraints is out of the scope of this paper.

The benefit of initialization is that we simplify the problem of constraint-guided clustering where we only need to focus on the *cannot-link* constraints in the optimization process as described in the following subsection. Another ben-

2.2 SCREEN_{PROJ} - A Constraint-Guided Feature Projection

In the previous work [5, 26], the pairwise constraints were used for learning an adaptive metric between the prototype of instances. However, learning a distance metric among high-dimensional instances is very time consuming. More importantly, recent research on high-dimensional space has shown that the concept of distance in high-dimensional space may not be meaningful [7]. Instead of using constraintguided metric learning, in this paper we propose a constraintguided feature projection approach (SCREEN_{PROJ}) to further improve the performance of semi-supervised clustering in the high-dimensional datasets. The objective is to learn the projection matrix $F_{d \times k} = \{F_1, \ldots, F_k\}$ containing k orthogonal unit-length d-dimensional vectors, which can project the original datasets into a low-dimensional space such that the distance between any pair of instances involved in the *cannot-link* constraints are maximized while the distance between any pair of instances involved in the must-link constraints are minimized. The objective function we try to maximize is:

$$f = \sum_{(x_1, x_2) \in C_{CL}} \|F^T(x_1 - x_2)\|^2 - \sum_{(x_1, x_2) \in C_{ML}} \|F^T(x_1 - x_2)\|^2$$
(1)

subject to the constraints

$$F_i^T F_j = \begin{cases} 1 & \text{if } i = j \\ 0 & \text{if } i \neq j \end{cases}$$
(2)

where $\|\cdot\|$ denotes L_2 norm and F is the projection matrix whose column vectors are orthogonal to each other.

As we described in Section 2.1, by applying the initialization methods shown in Figure 2, we can eliminate each transitive closure from *must-link* constraints with its equivalent average instance. Then, the objective function in Equation (1) can be further reduced to:

$$f = \sum_{(x'_1, x'_2) \in C'_{CL}} \|w_1 w_2 \cdot F^T (x'_1 - x'_2)\|^2$$
(3)

where $\{w_i\}_{i=1}^{N'}$ is the set of weights (which is measured by the number of instances in each transitive closure) for the reduced instances after pre-processing to the *must-link* constraints and N' is the reduced size of instances $(N' \leq N)$.

Note that in Equation (3), we still adopt the Euclidean distance instead of the cosine similarity as in the SPKM algorithm to calculate the objective value. This is because we work on the unit-length instances that satisfy the property in the following equation:

$$\|x - \mu\|^{2} = \|x\|^{2} + \|\mu\|^{2} - 2x^{T}\mu = 2 - 2x^{T}\mu \qquad (4)$$

From Equation (4), we can see that using the cosine similarity is equivalent to using the Euclidean distance when operating on the unit-length instances.

There exists an analytical solution to the above optimization problem of finding the optimal projection matrix F in Equation (3). The following theorem shows that the optimal projection matrix F is given by the first k eigenvectors of the covariance matrix $M_{d\times d}$ for a difference matrix $C_{d\times m}$, where each column of C is a weighted difference vector $w_1w_2 \cdot (x'_1 - x'_2) \in \mathbb{R}^d$ for a pair (x'_1, x'_2) in C'_{CL} and m is the number of pairs of *cannot-link* constraints.

THEOREM 1. Given the desired dimensionality k (k < d), the set of cannot-link constraints C'_{CL} , and the covariance matrix M = cov(C) (where C is defined as above), the optimal projection matrix $F_{d \times k}$ is comprised of the first k eigenvectors of M corresponding to the k largest eigenvalues.

PROOF. Consider the objective function

$$f = \sum_{\substack{(x'_1, x'_2) \in C'_{CL} \\ (x'_1, x'_2) \in C'_{CL} \\ = \sum_{\substack{(x'_1, x'_2) \in C'_{CL} \\ (x'_1, x'_2) \in C'_{CL} \\ = \sum_l F_l^T \left[\sum_{\substack{(x'_1, x'_2) \\ \in C'_{CL} \\ \in C'_{CL} \\ \in C'_{CL} \\ = \sum_l F_l^T (CC^T) F_l = \sum_l F_l^T MF_l \right]^2$$

where F_l 's are subject to constraints $F_l^T F_h = 1$ for l = h and 0 otherwise.

Using the traditional Lagrange multiplier optimization technique, we write the Lagrangian

$$L_{F_1,\dots,F_k} = f(F_1,\dots,F_k) - \sum_{l=1}^k \xi_l (F_l^T F_l - 1) .$$
 (5)

By taking the partial derivative of L_{F_1,\ldots,F_k} with respect to each F_l and setting it to zero, we get

$$\frac{\partial L}{\partial F_l} = 2MF_l - 2\xi_l F_l = 0 \qquad \forall l = 1, \dots, k$$

$$\Rightarrow MF_l = \xi_l F_l \qquad \forall l = 1, \dots, k .$$
(6)

It is clear from Equation (6) that solution F_l is an eigenvector of M and ξ_l is the corresponding eigenvalue of M. To maximize f, F must be the first k eigenvectors of M which makes f the sum of the k largest eigenvalues of M. \Box

After the constraint-guided feature projection as described above, we can represent the original instances in a lowdimensional space which conforms to the class information given in the form of pairwise constraints.

2.3 Constrained Spherical K-means

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Since we eliminate the *must-link* constraints and shrink the original dataset in the initialization step, our version of constrained spherical K-means for semi-supervised clustering is slightly different from the one as shown in [25]. In this section, we introduce our version of constrained spherical K-means algorithm for semi-supervised clustering.

Given a set of reduced instances $\mathcal{X}' = \{x'_1, \ldots, x'_{N'}\}$ with the corresponding weights $\mathcal{W} = \{w_1, \ldots, w_{N'}\}$, a set of *cannot-link* constraints, and a pre-specified number of clusters K, we aim to find K disjoint partitions. As shown in [12], finding a feasible solution for the *cannot-link* constraints is much harder than that for the *must-link* constraints. It is computationally intractable to find an exact

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cluster assignment which does not break any *cannot-link* constraints. Therefore, we adopt a local greedy heuristic to update cluster centroids as follows.

Given each *cannot-link* constraint $(x'_i, x'_j) \in C_{CL}$, we find two different cluster centroids $\mu_{x'_i}$ and $\mu_{x'_i}$ such that

$$w_{i} \cdot x_{i}^{T} \mu_{x_{i}} + w_{j} \cdot x_{j}^{T} \mu_{x_{j}}$$
(7)

is maximized and assign x'_i and x'_j to these two different centroids to avoid violating the *cannot-link* constraint. Figure 3 shows the pseudo-code of our Pairwise Constrained Spherical K-means (PCSKM) clustering algorithm.

Algorithm: The Pairwise Constrained Spherical K-means (PCSKM) Clustering Algorithm Input: Set of unit-length instances $\mathcal{X}' = \{x'_i\}_1^{N'}$, set of corresponding weight $\mathcal{W} = \{w_i\}_1^{N'}$, set of cannot-link constraints $C_{CL} = \{(x'_i, x'_j)\}$, and number of clusters K. Output: K partitions of the instances. Steps:

- 1. Initialize the K unit-length cluster centroids $\{\mu_h\}_{h=1}^K,$ set $t \leftarrow 1$
- 2. Repeat until convergence For i = 1 to m
 - (a) For each instance x'_i which does not involve in any cannot-link constraint, find the closest centroid $y_n = \arg \max_k x'_i^T \mu_k$;
 - (b) For each pair of instances (x'_i, x'_j) involved in *cannot-link* constraint, find two different centroids μ_k and $\mu_{k'}$ which maximize $w_i \cdot x'_i^T \mu_k + w_j \cdot x'_j^T \mu_{k'}$;
 - (c) For cluster k, let $\mathcal{X}'_k = \{x'_i | y_i = k\}$, the centroid is estimated as $\mu_k = \sum_{x \in \mathcal{X}'_k} / || \sum_{x \in \mathcal{X}'_k} ||$;

3. $t \leftarrow t+1$;

Figure 3: The Pairwise Constrained Spherical Kmeans Clustering Algorithm.

It is worth noting that our algorithm for semi-supervised clustering differs from the one used in [5] in that we do not consider the relative importance among *cannot-link* constraints, and we do not utilize pairwise constraints to supervise the cluster centroids initialization. However, these techniques can be easily incorporated into our algorithm.

Finally, an overview of our SCREEN method is shown in Figure 4. Please note that since the pre-process step to the pairwise constraints will shrink the original dataset, we need to post-process the resultant K partitions (clusters) in order to be in accordance with the original dataset.

3. EXPERIMENTAL RESULTS

In this section, we study the performance of the SCREEN method. Specifically, we demonstrate: (1) the effectiveness of constraint-guided feature projection, (2) the relative impact of Must-link and Cannot-link constraints on the performance of the SCREEN method, (3) the choice of reduced dimensionality, (4) the computational performance of the SCREEN method, and (5) the clustering performance of SCREEN, compared with several existing semi-supervised clustering algorithms.

Algorithm: SCREEN

Input: Set of unit-length instances $\mathcal{X}' = \{x_i\}_1^{N'}$, set of corresponding weight $\mathcal{W} = \{w_i\}_1^{N'}$, set of *cannot-link* constraints $C_{CL} = \{(x'_i, x'_j)\}$, and number of clusters K.

Output: *K* partitions of the instances.

Steps:

1. $\mathcal{X}' = \text{SCREEN}_{PROJ}(\mathcal{X}, \mathcal{W}, C_{CL})$

- 2. $\mathcal{X}'_k = \text{PCSKM}(\mathcal{X}', \mathcal{W}, C_{CL})$, where $k = 1, \dots, K$
- 3. post-process \mathcal{X}'_k to be in accordance with the original instances $\mathcal X$

Figure 4: An Overview of the SCREEN Method.

3.1 The Experimental Setup

Experimental Datasets. Our experiments were performed on a couple of real-world datasets from different application domains. There are six UCI datasets $^{1}[20]$, six datasets derived from TREC collections 2 and nine datasets constructed from 20-Newsgroup [18]. The descriptions of these data sets are summarized as follows.

- 1. Six UCI datasets: balance-scale, ionosphere, iris, soybean, vehicle, and wine. Those datasets have been used in learning a distance metric [26] and the work on the constrained feature projection via RCA [3]. We use these relatively low-dimensional datasets to demonstrate the performance of SCREEN_{PROJ}, in comparison with other dimensionality reduction methods such as PCA and RCA.
- 2. Six data sets: tr11, tr12, tr23, tr31, tr41, and tr45 from the TREC collection are used to compare the performance of SCREEN_{PROJ} with PCA and RCA on highdimensional datasets. These datasets are available in the CLUTO toolkit [17].
- 3. In order to evaluate the overall performance of our SCREEN method, we also compare it with the stateof-the-art, semi-supervised clustering algorithms including the constrained metric learning method [26] and the HMRF-Kmeans algorithm [4] on the nine datasets of the 20-Newsgroup corpus. The 20-Newsgroup data consists of approximately 20,000 newsgroup articles collected evenly from 20 different Usenet newsgroups. Many of the newsgroups share similar topics and about 4.5% of the documents are cross-posted over different newsgroups making the class boundary rather fuzzy. We applied the same pre-processing steps as in [13], i.e., removed stop words, ignored file headers, subject line and selected the top 2000 words by mutual information. Specific details of the datasets are given in Table 2. The Bow [19] library is used in generating those datasets from the 20-Newsgroup corpus.

Evaluation Measures. In this paper, we use *normalized mutual information* (NMI) as the clustering validation measure. NMI, an external validation metric, estimates the quality of clustering with respect to the given true labels of

 $^{^{1}} http://www.ics.uci.edu/~mlearn/MLRepository.html ^{2} http://trec.nist.gov$

Dataset	Newsgroup included	Group doc.	Tot. doc.
Binary _{1,2,3}	talk.politics.mideast, talk.politics.misc	250	500
$Multi5_{1,2,3}$	comp.graphics, rec.motorcycles,	100	500
	rec.sports.baseball, sci.space,		
	talk.politics.mideast		
$Multi10_{1,2,3}$	alt.atheism, comp.sys.mac.hardware,	50	500
	misc.forsale, rec.autos,		
	rec.sport.hockey, sci.crypt,		
	sci.electronics, sci.med,		
	sci.space, talk.politics.gun		

Table 2: Nine Datasets from the 20-Newsgroup Corpus.

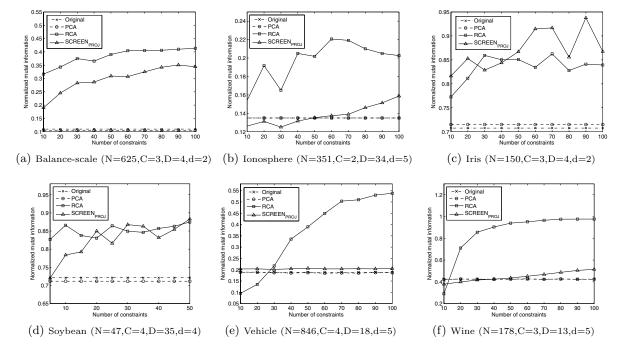


Figure 5: The clustering performance on six UCI datasets with different numbers of constraints (N: size of dataset; C: number of clusters; D: dimensionality of original data; d: reduced dimensionality after projection).

the datasets [24]. If \hat{Z} is the random variable denoting the cluster assignments of the instances and Z is the random variable denoting the underlying class labels, then NMI is defined as

$$NMI = \frac{I(Z;Z)}{(H(\hat{Z}) + H(Z))/2}$$
(8)

where $I(\hat{Z}; Z) = H(Z) - H(Z|\hat{Z})$ is the mutual information between the random variables \hat{Z} and Z, H(Z) is the Shannon entropy of Z, and $H(Z|\hat{Z})$ is the conditional entropy of Z given \hat{Z} [11]. The range of NMI values is 0 to 1. In general, the larger the NMI value is, the better the clustering quality is. NMI is better than other external clustering validation measures such as purity and entropy, since it does not necessarily increase when the number of clusters increases.

Finally, we implemented the SCREEN algorithm in Matlab and conducted our experiments on a machine with 4 Intel Xeon 2.8 GHz CPUs and 2G main memory running under the GNU/Linux operating system. For each test dataset, we repeated experiments for 20 trials. For the UCI datasets, we randomly generated 100 pairwise constraints in each trial. For the Trec datasets and data sets from the 20-Newsgroup collection, we randomly generated 500 pairwise constraints from half of the dataset, and tested the performance on the whole dataset. Also, the final result is the average of the results from the 20 trials.

3.2 The Effectiveness of SCREEN_{PROJ}

In this section, we compare SCREEN_{PROJ} with some existing dimensionality reduction methods such as PCA and RCA³. In order to do a thorough comparison, we used both relatively low-dimensional datasets from the UCI repository and high-dimensional datasets from the Trec corpus. For the low-dimensional UCI datasets, we used the standard Kmeans algorithm as the baseline clustering algorithm. For

³Thanks to the authors for providing their code on-line at http://www.cs.huji.ac.il/~tomboy/code/RCA.zip for [3]

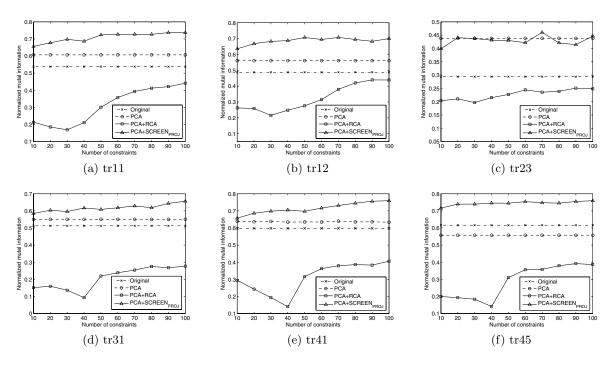


Figure 6: Clustering performance on 6 Trec datasets with different numbers of constraints.

the high-dimensional Trec datasets, we chose the spherical K-means algorithm [14] instead.

For six UCI datasets, Figure 5 shows the clustering performance of standard K-means applied to the original as well as projected data by different dimension reduction algorithms with different numbers of pairwise constraints. As can be seen, RCA performs well on low-dimensional data. Also, the performance of RCA significantly improves as the number of available constraints increases. However, we can also observe that the performance of RCA can be worse than that of PCA when there is a small number of constraints in the datasets such as *Vehicle* and *Wine* (we know that PCA is unsupervised and does not use any pairwise constraints). In contrast, the performance of SCREEN_{PROJ} is always comparable to, or better than that of PCA. Finally, we observe that the performance of SCREEN_{PROJ} is comparable to that of RCA on *Soybean* and *Iris* datasets.

However, our experiments on six high-dimensional Trec data sets show that the performance of RCA heavily depends on the dimensionality of the original data. Also, it is computationally expensive to directly apply RCA to highdimensional datasets. Indeed, for data sets with extremely high dimensions, we need to first reduce their dimension to a lower level before applying the RCA method. Therefore, for the purpose of a fair comparison, we first used PCA to project the original data into a 100-dimensional space, and then applied the different algorithms to further reduce the dimensionality to 30. Figure 6 shows the results of this experiment on six Trec datasets. In the figure, we observe that $SCREEN_{PROJ}$ nearly always achieves the best performance on all six test datasets. In contrast, although we first reduce the dimension of six data sets to 100 using PCA, the performance of RCA is still the worst among all the algorithms. In other words, RCA may not be a good dimension reduction method for high-dimensional data.

3.3 Must-link vs. Cannot-link

Here, we compare the relative impact of *must-link* and *cannot-link* constraints on the performance of the SCREEN method. In this experiment, we incorporate a parameter β to the objective function in Equation (3) to adjust the relative impact between *must-link* and *cannot-link* constraints:

$$f = (1 - \beta) \cdot \sum_{(x_1, x_2) \in C_{CL}} \|F^T(x_1 - x_2)\|^2 -\beta \cdot \sum_{(x_1, x_2) \in C_{ML}} \|F^T(x_1 - x_2)\|^2$$
(9)

From Equation (9), we observe that $\beta = 0$ is equivalent to only using *cannot-link* constraints in finding the optimal feature projection matrix. When $\beta = 1$, we only use *mustlink* constraints to perform the feature projection. In our experiments, we varied the value of β in steps of 0.1 from 0 to 1. The clustering results, as measured by NMI, are plotted in Figure 7 with respect to different values of β . In the figure, the *x*-axis denotes the different values of parameter β and the *y*-axis denotes the clustering performance measured by NMI.

As can be seen in Figure 7, there is no significant difference on the clustering performance when β is in the range of 0.1 to 0.9. However, when using only *must-link* constraints ($\beta = 1$) the clustering performance deteriorates sharply. This indicates that the *cannot-link* constraints are more important than the *must-link* constraints in guiding the feature projection to get meaningful representation for each instance in the low-dimensional space.

3.4 The Choice of Dimension k

In this section, we empirically evaluate the impact of different number of reduced dimension k on the performance of

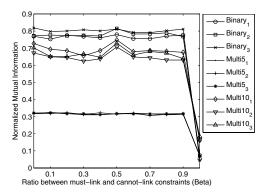


Figure 7: The relative impact of must-link and cannot-link constraints.

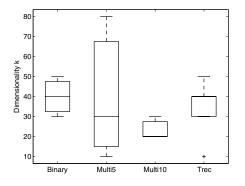


Figure 8: The Choice of Reduced Dimension k.

the SCREEN method. Specifically, we test the performance of SCREEN in terms of NMI with respect to different values of k varing from 10 to 100. Given a specified k, we repeat experiments 20 times. In each trial, we randomly generate 250 pairwise constraints as additional information. The experimental results on the datasets from 20-Newsgroup and Trec collections are shown in Figure 8 as four boxplots, which corresponds to the experimental results on sub-datasets from Binary, Multi5, Multi10, and Trec.

There are three sub-datasets: $Binary_1$, $Binary_2$, and $Binary_3$ from the Binary data collection. The Binary boxplot shows the k values when SCREEN achieves the best clustering performance on these three sub-datasets. Also, the Multi5 boxplot shows the k values when SCREEN has the best clustering performance on three sub-datasets: $Multi5_1$, $Multi5_2$, $Multi5_3$. In addition, the Multi10 boxplot presents the k values for the case that SCREEN has the best clustering performance on three sub-datasets: $Multi10_2$, $Multi10_3$. Finally, there are six sub-datasets: tr11, tr12, tr23, tr31, tr41, and tr45 from the Trec corpus. The Trec boxplots shows six k values which lead to the best clustering performance of SCREEN on these datasets.

In Figure 8, we observe that SCREEN achieves the best performance at different k values for different datasets. However, we notice that the clustering performance is maximized when the median of k values is between k = 20 and k = 40. In all our experiments, we use this as a guideline for the choice of k values.

3.5 Computational Performance

In the following two subsections, we evaluate the overall computational and clustering performance of our SCREEN method. The benchmark algorithms are listed as follows.

- SPKM: the standard spherical K-means algorithm [14] which does not use pairwise constraints. It is worth noting that the method proposed in this paper is tailored for high-dimensional sparse data with directional characteristics, which mainly stem from text documents represented by the vector space model (VSM) [6]. The most relevant work in this application domain is SPKM, which adapts the standard K-means algorithm to cluster the normalized unit-length instances by using the cosine similarity as the proximity function. Hence, we chose SPKM as the baseline;
- PCSKM: the pairwise constrained spherical K-means algorithm described in Figure 3, which can be regarded as another implementation of semi-supervised, constrained K-means described in [25];
- PCSKM+M: the pairwise constrained spherical K-means algorithm preceded by an additional metric learning to get an adaptive distance between instances, which is proposed by Xing et al. [26];
- MPCSKM: the HMRF-Kmeans algorithm proposed by Basu et al [5]. This algorithm unifies the metric learning and constrained clustering into a general probabilistic framework⁴.

First, we evaluate the computational performance of the semi-supervised clustering algorithms on the selected 20-Newsgroup datasets with respect to different numbers of pairwise constraints. Due to the space limit, for each category of the datasets we only give out one result since the datasets from the same category usually lead to similar outputs. The experimental results are summarized in Figure 9, where the x-axis denotes the number of pairwise constraints and the y-axis denotes the elapsed running time in log scale. Please note that since the MPCSKM algorithm is not implemented in Matlab, we did not include this algorithm for this comparison.

As demonstrated in Figure 9, the execution time of SPKM is consistently the lowest among all the methods since it does not perform extra work in addition to enforcing the clustering process based on the pairwise constraints. The PC-SKM+M algorithm via metric learning method is always the slowest when compared to other methods. This is because the metric learning method has to learn a different weight for each individual dimension. When the dimensionality is very high, the cost of metric learning will be very high compared to the constraint-guided feature projection. In Figure 9, we can see that the SCREEN method, which utilizes the feature projection method, is only slightly slower than the PCSKM algorithm due to the extra work on the supervised dimensionality reduction, but much faster than that of PCSKM+M algorithm. This is because it only involves an eigen value decomposition of a covariance matrix formed by *cannot-link* constraints, which can be implemented efficiently by Singular Value Decomposition (SVD). In addition, one can still explore some iterative methods, such as

⁴Thanks to the authors for putting their implementation on-line at http://www.cs.utexas.edu/users/ml/risc/ for [5].

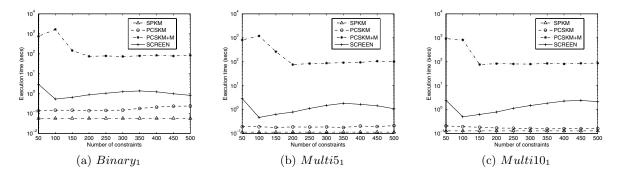


Figure 9: A Comparison of Computational performance using 20-Newsgroup datasets.

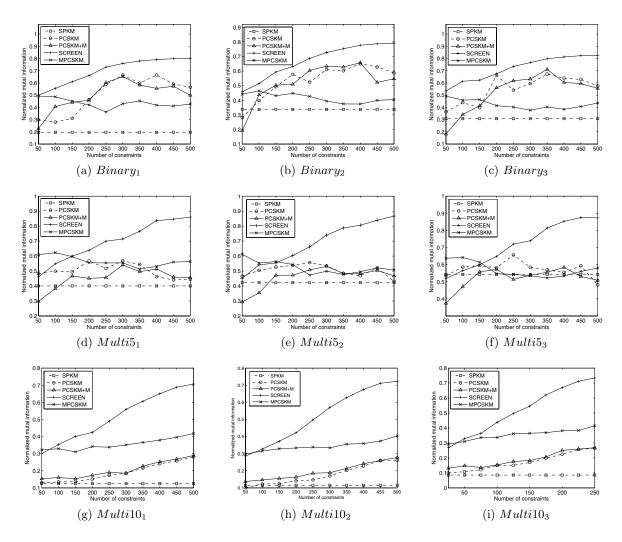


Figure 10: A Comparison of Clustering performance using 20-Newsgroup datasets.

EM algorithm for PCA [23] or Nystrom method [9], to further improve the efficiency.

3.6 A Comparison of Clustering Performance

Here, we compare the clustering performance of various semi-supervised clustering algorithms. The results are shown in Figure 10, where the x-axis denotes the number of pairwise constraints, and the y-axis denotes the clustering performance in terms of NMI. We have tested various values of k - the number of reduced dimension. Due to the space limit, we select k = 30 to report the results.

In general, it is clear that on most datasets, the clustering performance of all algorithms constantly improve with the increase of the number of pairwise constraints. However, the clustering performance of the SCREEN method is more stable compared to the other methods, and always outperforms the PCSKM+M algorithm via metric learning and MPCSKM algorithm via HMRF model. This is mainly due to the fact that constraint-guided feature projection can easily produce more condensed and meaningful representations for each instance. In addition, PCSKM+M is not much better than the PCSKM algorithm except for the Multi10 dataset. This is because it is a big challenge for metric learning to learn a reasonable distance measure between any pair of sparse instances in the original high-dimensional space.

4. RELATED WORK

The related literature on semi-supervised clustering can be grouped into three categories: constraint-based methods, distance-based methods, and a combination of constraintbased and distance-based methods.

For constraint-based methods, the cop-kmeans algorithm [25] guides the cluster allocation process by a constraint motivated heuristic objective function. However, this algorithm strictly enforces the clustering process such that any violation of the given pairwise constraints is forbidden, which limits its use, especially in a noisy environment. In contrast, our version of semi-supervised clustering algorithm allows some relaxation of the pairwise constraints. Also, Basu et al. [4] proposed a seeded K-means which tries to get better initial cluster centroids from the labeled instances in addition to constraining the clustering process, while their supervised cluster initialization is based on the labeled instances instances instead of pairwise constraints.

For distance-based methods, Cohn et al. [10] used gradient descent for weighted Jensen-Shannon divergence in the context of EM clustering. Xing et al. [26] combined the Newton Raphson method and iterative projection together to learn a Mahalanobis distance for K-means clustering. De Bie et al. [8] proposed a more efficient algorithm for learning the distance metric with side information, which utilized Canonical Correlation Analysis (CCA) to approximate LDA. In general, the metric learning used in the *distance*based method, which is equivalent to learning an adaptive weight for each dimension, is either based on iterative algorithms, such as gradient descent and Newton's method, or involves some matrix operations. However, the distancebased method has high computational cost when applied to the high-dimensional data. Indeed, data represented in matrix is often singular when the sparsity of the data is high. This makes some matrix operations, such as inversion, computationally intractable.

For hybrid methods, Basu et al. [5] introduced a general probabilistic framework which unifies the *constraint-based* and *distance-based* method into the Hidden Markov Random Field (HMRF). The proposed HMRF-EM algorithm can interweave the constrained clustering and distance learning interactively in the process of semi-supervised clustering.

Also, the related literature on feature reduction includes Principle Component Analysis (PCA) [22] which tries to find a low rank approximation to represent the high-dimensional data, and Fisher's Linear Discriminant Analysis (LDA) [15] which tries to find one or more directions along which different classes can be best separated while the variance of each class is minimized given the label for each instance. The PCA method works in an unsupervised manner where the class information is not available, which makes the reduced dataset incapable of capturing the original class information. In contrast, the LDA method needs to know the exact information in order to calculate the between/within-class scatter matrix. Our constraint-guided feature projection method differs from the traditional LDA method in that we incorporate a more general supervision in the form of pairwise constraints instead of the complete class information which may be unavailable in certain application domains. To the best of our knowledge, the most related work is the Relevant Component Analysis (RCA) algorithm [3], which is based only on *must-link* constraints and tries to learn a Mahalanobis distance using Whitening transform [16].

In this paper, our major focus is to provide an alternative way to improve the semi-supervised clustering for high-dimensional sparse data by constraint-guided feature projection instead of metric learning. Existing approaches for clustering high-dimensional data usually involve the use of feature projection and feature selection. Feature projection techniques, as we described above, attempt to represent a dataset by its latent variables which are usually much fewer than the number of original features. Feature selection methods select only the most relevant dimensions from a dataset to summarize its instances. The typical algorithms of feature selection include "wrapper methods" and "filter methods". The recently proposed subspace clustering algorithm [21] can be regarded as an extension to the feature selection methods which attempts to find clusters in different subspaces of the same datasets. Existing subspace clustering algorithm can be grouped into two categories: the top-down method such as projected clustering [1] and the bottom-up method such as CLIQUE [2] etc. An excellent survey on techniques of subspace clustering is available in [21]. It is worth noting that the recently proposed method on semi-supervised projected clustering [27] utilized the limited supervision in the form of labeled instance in subspace clustering. The motivation of this work is to find a more compact representation for each cluster to efficiently represent the instances within it. Also, they used feature selection instead of feature projection in applying the supervision in each cluster. This is different from our method.

5. CONCLUSIONS AND FUTURE WORK

In this paper, we proposed a Semi-supervised Clustering method based on spheRical K-mEans via fEature projectioN (SCREEN), which is tailored for handling sparse, highdimensional, data. Specifically, the SCREEN method first uses the constraint-guided feature projection to reduce the dimensionality and then applies the constrained spherical K-means algorithm to cluster data with reduced dimension.

In the development of the SRCEEN method, we formulate the problem of constraint-guided feature projection as an optimization problem. The goal is to find a feature projection matrix based on the pairwise instance constraints, and give an analytical solution which can be implemented without too much effort. In addition, for the constrained spherical K-means algorithm, we introduce a heuristic solution to loosely enforce the pairwise constraints, which enable it to be applied in much wider application domains.

Finally, we have compared the SCREEN method with existing semi-supervised clustering methods using real-world datasets. The experimental results indicate that SCREEN can achieve a better clustering performance with a smaller computational cost. We also studied the relative impact of *must-link* and *cannot-link* constraints in guiding the clustering process. Our analysis shows that the *cannot-link* con-

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straints are more important than the *must-link* constraints in providing meaningful class information.

There are several potential directions for future research. First, we are interested in automatically identifying the right number for the reduced dimensionality based on the background knowledge other than providing a pre-specified value. Second, we plan to explore alternative methods to employ supervision in guiding the unsupervised clustering, e.g., supervised feature clustering.

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